

AS Level Mathematics A H230/02 Pure Mathematics and Mechanics Sample Question Paper

Date – Morning/Afternoon

Time allowed: 1 hour 30 minutes

OCR supplied materials:

Printed Answer Booklet

You must have:

- Printed Answer Booklet
- Scientific or graphical calculator



INSTRUCTIONS

- Use black ink. HB pencil may be used for graphs and diagrams only.
- Complete the boxes provided on the Printed Answer Booklet with your name, centre number and candidate number.
- Answer **all** the questions.
- **Write your answer to each question in the space provided in the Printed Answer Booklet.**
- Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Do **not** write in the bar codes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.
- The acceleration due to gravity is denoted by $g \text{ m s}^{-2}$. Unless otherwise instructed, when a numerical value is needed, use $g = 9.8$.

INFORMATION

- The total number of marks for this paper is **75**.
- The marks for each question are shown in brackets [].
- **You are reminded of the need for clear presentation in your answers.**
- The Printed Answer Booklet consists of **12** pages. The Question Paper consists of **8** pages.

Formulae
AS Level Mathematics A (H230)

Binomial series

$$(a+b)^n = a^n + {}^n C_1 a^{n-1}b + {}^n C_2 a^{n-2}b^2 + \dots + {}^n C_r a^{n-r}b^r + \dots + b^n \quad (n \in \mathbb{N}),$$

$$\text{where } {}^n C_r = \binom{n}{r} = \frac{n!}{r!(n-r)!}$$

Differentiation from first principles

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

Standard deviation

$$\sqrt{\frac{\sum(x-\bar{x})^2}{n}} = \sqrt{\frac{\sum x^2}{n} - \bar{x}^2} \quad \text{or} \quad \sqrt{\frac{\sum f(x-\bar{x})^2}{\sum f}} = \sqrt{\frac{\sum fx^2}{\sum f} - \bar{x}^2}$$

The binomial distribution

If $X \sim B(n, p)$ then $P(X = x) = \binom{n}{x} p^x (1-p)^{n-x}$, Mean of X is np , Variance of X is $np(1-p)$

Kinematics

$$v = u + at$$

$$s = ut + \frac{1}{2}at^2$$

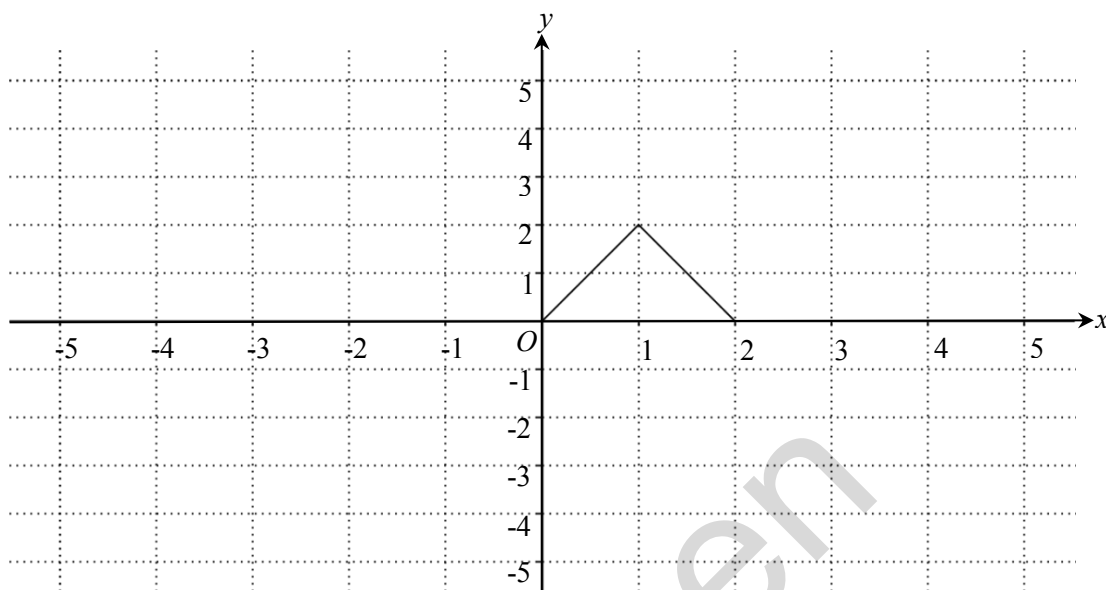
$$s = \frac{1}{2}(u+v)t$$

$$v^2 = u^2 + 2as$$

$$s = vt - \frac{1}{2}at^2$$

Section A: Pure Mathematics
Answer **all** the questions

- 1 (i) The diagram below shows the graph of $y = f(x)$.



- (a) On the diagram in the Printed Answer Booklet draw the graph of $y = f(x + 3)$. [2]
- (b) Describe fully the transformation which transforms the graph of $y = f(x)$ to the graph of $y = -f(x)$. [1]
- (ii) The point $(2, 3)$ lies on the graph of $y = g(x)$. State the coordinates of its image when $y = g(x)$ is transformed to
- (a) $y = 4g(x)$, [1]
- (b) $y = g(4x)$. [1]

- 2 In this question you must show detailed reasoning.

Solve the equation $2\cos^2 x = 2 - \sin x$ for $0^\circ \leq x \leq 180^\circ$. [5]

- 3 The number of members of a social networking site is modelled by $m = 150e^{2t}$, where m is the number of members and t is time in weeks after the launch of the site.
- (i) State what this model implies about the relationship between m and the rate of change of m . [2]
 - (ii) What is the significance of the integer 150 in the model? [1]
 - (iii) Find the week in which the model predicts that the number of members first exceeds 60 000. [3]
 - (iv) The social networking site only expects to attract 60 000 members. Suggest how the model could be refined to take account of this. [1]
- 4 The points A , B and C have position vectors $\begin{pmatrix} -2 \\ 1 \end{pmatrix}$, $\begin{pmatrix} 2 \\ 5 \end{pmatrix}$ and $\begin{pmatrix} 6 \\ 3 \end{pmatrix}$ respectively. M is the midpoint of BC .
- (i) Find the position vector of the point D such that $\overrightarrow{BC} = \overrightarrow{AD}$. [3]
 - (ii) Find the magnitude of \overline{AM} . [3]

Specimen

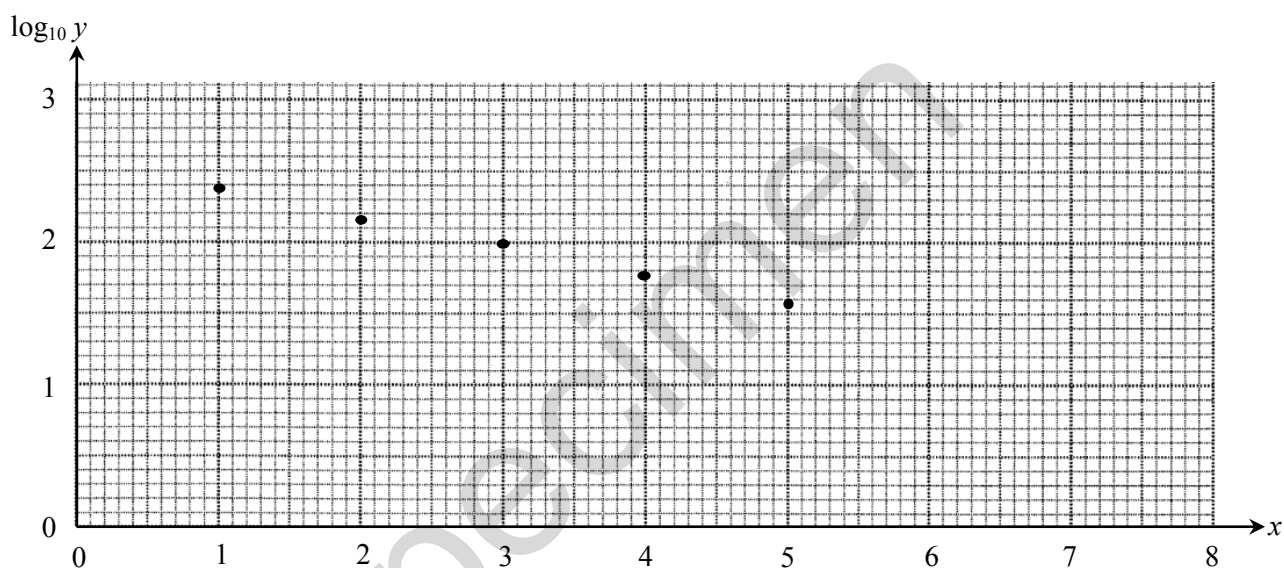
5 A doctors' surgery starts a campaign to reduce missed appointments. The number of missed appointments for each of the first five weeks after the start of the campaign is shown below.

| | | | | | |
|---|-----|-----|----|----|----|
| Number of weeks after the start (x) | 1 | 2 | 3 | 4 | 5 |
| Number of missed appointments (y) | 235 | 149 | 99 | 59 | 38 |

It was felt that this data could be modelled by an equation of the form $y = pq^x$ where p and q are constants.

- (i) Show that this relationship may be expressed in the form $\log_{10} y = mx + c$, expressing m and c in terms of p and/or q . [2]

The diagram below shows $\log_{10} y$ plotted against x , for the given data.



- (ii) Estimate the values of p and q . [3]
- (iii) Use the model to predict when the number of missed appointments will fall below 20. Explain why this answer may not be reliable. [2]

6 (i) A student suggests that, for any prime number between 20 and 40, when its digits are squared and then added, the sum is odd. For example, 23 has digits 2 and 3 which gives $2^2 + 3^2 = 13$, which is odd. Show by counter example that this suggestion is false. [2]

(ii) Prove that the sum of the squares of any three consecutive positive integers cannot be divided by 3. [3]

7 Differentiate $f(x) = x^4$ from first principles.

[5]

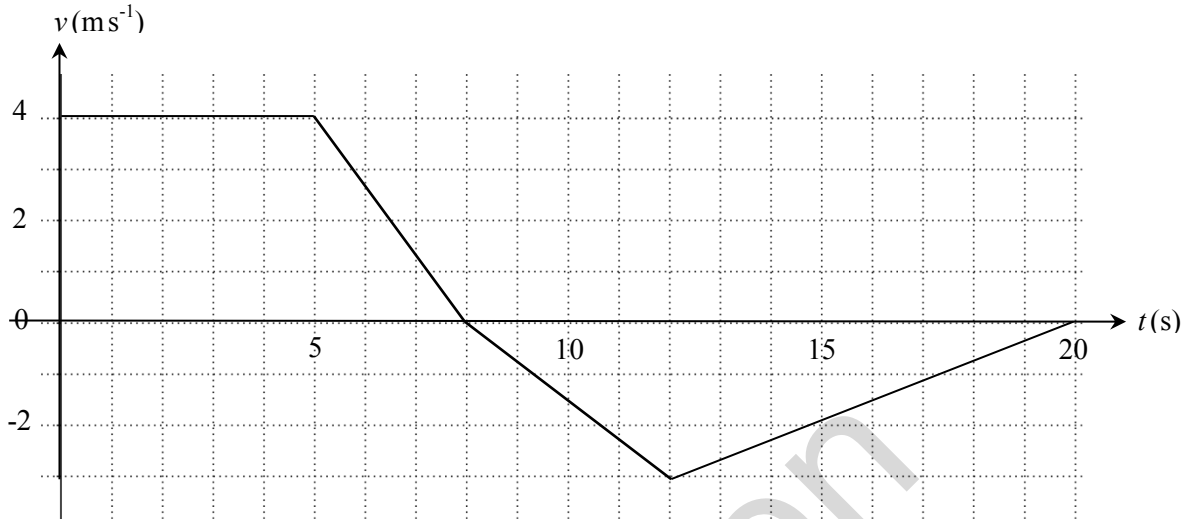
8 A curve has equation $y = kx^{\frac{3}{2}}$ where k is a constant. The point P on the curve has x -coordinate 4. The normal to the curve at P is parallel to the line $2x + 3y = 0$ and meets the x -axis at the point Q . The line PQ is the radius of a circle centre P .
Show that $k = \frac{1}{2}$. Find the equation of the circle.

[10]

Specimen

Section B: Mechanics
Answer **all** the questions

- 9 The diagram below shows the velocity-time graph of a car moving along a straight road, where $v \text{ ms}^{-1}$ is the velocity of the car at time t s after it passes through the point A .



- (i) Calculate the acceleration of the car at $t = 6$. [2]
- (ii) Jasmit says “The distance travelled by the car during the first 20 seconds of the car’s motion is more than five times its displacement from A after the first 20 seconds of the car’s motion”. Give evidence to support Jasmit’s statement. [3]
- 10 A student is attempting to model the flight of a boomerang. She throws the boomerang from a fixed point O and catches it when it returns to O . She suggests the model for the displacement, s metres, after t seconds is given by $s = 9t^2 - \frac{3}{2}t^3$, $0 \leq t \leq 6$. For this model
- (i) determine what happens at $t = 6$, [2]
- (ii) find the greatest displacement of the boomerang from O , [4]
- (iii) find the velocity of the boomerang 1 second before the student catches it, [2]
- (iv) find the acceleration of the boomerang 1 second before the student catches it. [2]

- 11 In this question the unit vectors \mathbf{i} and \mathbf{j} are in the directions east and north respectively.

Distance is measured in metres and time in seconds.

A ship of mass 100 000 kg is being towed by two tug boats. The cables attaching each tug to the ship are horizontal. One tug produces a force of $(350\mathbf{i} + 400\mathbf{j})$ N and the other tug produces a force of $(250\mathbf{i} - 400\mathbf{j})$ N. The total resistance to motion is 200 N. At the instant when the tugs begin to tow the ship, it is moving east at a speed of 1.5 m s^{-1} .

- (i) Explain why the ship continues to move directly east. [2]
- (ii) Find the acceleration of the ship. [2]
- (iii) Find the time which the ship takes to move 400 m while it is being towed. Find its speed after moving that distance. [6]

END OF QUESTION PAPER

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...day June 20XX – Morning/Afternoon

AS Level Mathematics A

H230/02 Pure Mathematics and Mechanics

SAMPLE MARK SCHEME

Duration: 1 hour 30 minutes

MAXIMUM MARK 75



This document consists of 12 pages

Text Instructions

1. Annotations and abbreviations

| Annotation in scoris | Meaning |
|------------------------------------|--|
| ✓ and ✕ | |
| BOD | Benefit of doubt |
| FT | Follow through |
| ISW | Ignore subsequent working |
| M0, M1 | Method mark awarded 0, 1 |
| A0, A1 | Accuracy mark awarded 0, 1 |
| B0, B1 | Independent mark awarded 0, 1 |
| SC | Special case |
| ^ | Omission sign |
| MR | Misread |
| Highlighting | |
| | |
| Other abbreviations in mark scheme | Meaning |
| E1 | Mark for explaining a result or establishing a given result |
| dep* | Mark dependent on a previous mark, indicated by * |
| cao | Correct answer only |
| oe | Or equivalent |
| rot | Rounded or truncated |
| soi | Seen or implied |
| www | Without wrong working |
| AG | Answer given |
| awrt | Anything which rounds to |
| BC | By Calculator |
| DR | This question included the instruction: In this question you must show detailed reasoning. |

2. Subject-specific Marking Instructions for AS Level Mathematics A

- a Annotations should be used whenever appropriate during your marking. The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded. For subsequent marking you must make it clear how you have arrived at the mark you have awarded.
- b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner. If you are in any doubt whatsoever you should contact your Team Leader.
- c The following types of marks are available.

M

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

A

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

B

Mark for a correct result or statement independent of Method marks.

E

Mark for explaining a result or establishing a given result. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only – differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case please, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.
Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.
- f Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.) We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so. When a value is given in the paper only accept an answer correct to at least as many significant figures as the given value. This rule should be applied to each case. When a value is not given in the paper accept any answer that agrees with the correct value to 2 s.f. Follow through should be used so that only one mark is lost for each distinct accuracy error, except for errors due to premature approximation which should be penalised only once in the examination. There is no penalty for using a wrong value for g . E marks will be lost except when results agree to the accuracy required in the question.
- g Rules for replaced work: if a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests; if there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others. NB Follow these maths-specific instructions rather than those in the assessor handbook.
- h For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A mark in the question. Marks designated as cao may be awarded as long as there are no other errors. E marks are lost unless, by chance, the given results are established by equivalent working. 'Fresh starts' will not affect an earlier decision about a misread. Note that a miscopy of the candidate's own working is not a misread but an accuracy error.
- i If a calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers (provided, of course, that there is nothing in the wording of the question specifying that analytical methods are required). Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.
- j If in any case the scheme operates with considerable unfairness consult your Team Leader.

| Question | | | Answer | Marks | AOs | Guidance | |
|----------|------|-----|---|---|--|---|---|
| 1 | (i) | (a) | Coordinates $(-3, 0)$, $(-1, 0)$ and $(-2, 2)$ seen | M1 A1 [2] | 1.1 1.1 | A horizontal translation only is seen | |
| 1 | (i) | (b) | Reflection in the x -axis | B1 [1] | 1.2 | Must be a complete statement | |
| 1 | (ii) | (a) | $(2, 12)$ | B1 [1] | 1.1 | | |
| 1 | (ii) | (b) | $(\frac{1}{2}, 3)$ | B1 [1] | 1.1 | | |
| 2 | | | DR $2(1 - \sin^2 x) = 2 - \sin x$ $2\sin^2 x - \sin x = 0$ $\sin x(2\sin x - 1) = 0$ $\sin x = \frac{1}{2}$ so $x = 30$ or $x = 150$ $\sin x = 0$ so $x = 0$ or $x = 180$ | M1 A1 M1 A1 A1 [5] | 3.1a 1.1 1.1a 1.1 1.1 | Use $\cos^2 x = 1 - \sin^2 x$ and simplify Obtain $2\sin^2 x - 1\sin x = 0$ Attempt to solve a 2 term quadratic in $\sin x$ and use correct order of operations to obtain x Both values are required Both values are required | One step of simplification must be seen Use any valid method Must be seen |

| Question | | Answer | Marks | AOs | Guidance |
|----------|-------|---|---|---|--|
| 3 | (i) | The model is exponential so the rate of change of m is proportional to m In this case, the rate of change of m is $2m$ | M1 E1 [2] | 1.1 2.2a | Gradient of $e^{kx} = ke^{kx}$ In context |
| 3 | (ii) | The initial membership | B1 [1] | 1.1 | |
| 3 | (iii) | $60000 = 150e^{2t}$ $\ln 400 = 2t$ $2.995 = t$ and hence 3 | M1 A1 A1 [3] | 3.4 1.1 1.1 | Correct equation and use correct order of operations Obtain correct intermediate step Or $\ln 60000 = \ln 150 + 2t$ Obtain correct answer |
| 3 | (iv) | E.g. When the graph reaches 60 000 the graph becomes constant. | B1 [1] | 3.5c | Correct suggestion |
| 4 | (i) | $\vec{BC} = \begin{pmatrix} 4 \\ -2 \end{pmatrix}$ $\begin{pmatrix} 4 \\ -2 \end{pmatrix} = \begin{pmatrix} x \\ y \end{pmatrix} - \begin{pmatrix} -2 \\ 1 \end{pmatrix} = \mathbf{d} - \mathbf{a} = \vec{AD}$ $\vec{OD} = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$ | B1 M1 A1 [3] | 1.1 3.1a 1.1 | soi |
| 4 | (ii) | $\vec{OM} = \begin{pmatrix} 4 \\ 4 \end{pmatrix}$ $\vec{AM} = \vec{OM} - \vec{OA} = \begin{pmatrix} 6 \\ 3 \end{pmatrix}$ $ \vec{AM} = \sqrt{6^2 + 3^2} = 3\sqrt{5}$ | B1 M1 A1 [3] | 1.1 1.1 2.2a | soi Accept 6.71 |

| Question | | Answer | Marks | AOs | Guidance |
|----------|-------|---|--|--|---|
| 5 | (i) | $\log_{10} y = \log_{10} p + x \log_{10} q$ $m = \log_{10} q, c = \log_{10} p$ | B1 B1 [2] | 2.1 2.4 | |
| 5 | (ii) | E.g. $\log_{10} q = \frac{2.4-1.6}{1-5} = -0.2$ $q = 10^{-0.2} = 0.63$ $\log_{10} p = 2.5$ so $p = 380$ | M1 A1 B1 [3] | 3.3 1.1 1.1 | Measure gradient from graph and identify it as $\log q$ Accept q in $[0.6, 0.7]$ Accept p in $[320, 400]$ |
| 5 | (iii) | $\log_{10} 20 = 1.3$ so week 7 E.g. Extrapolation is unjustified because it assumes that the assumptions made in the model will hold true in the long term | B1 E1 [2] | 3.4 3.5b | One valid explanation |
| 6 | (i) | 31 gives $3^2 + 1^2 = 10$ 10 is even and hence the suggestion is false | M1 E1 [2] | 2.1 2.1 | OR M1 37 gives $3^2 + 7^2 = 58$ E1 58 is even and hence the suggestion is false |
| 6 | (ii) | $n^2 + (n+1)^2 + (n+2)^2$ $3n^2 + 6n + 5$ $3(n^2 + 2n + 1) + 2$ which always leaves a remainder of 2 and so cannot be divided by 3 | M1 A1FT E1 [3] | 2.1 1.1 2.1 | Any valid expressions for three consecutive integers FT <i>their</i> expressions Correct conclusion. |

| Question | Answer | Marks | AOs | Guidance |
|----------|--|--|---|---|
| 7 | $f(x+h) = x^4 + 4x^3h + 6x^2h^2 + 4xh^3 + h^4$ $\frac{f(x+h) - f(x)}{h} = \frac{4x^3h + 6x^2h^2 + 4xh^3 + h^4}{h}$ $= 4x^3 + 6x^2h + 4xh^2 + h^3$ <p>As $h \rightarrow 0$ all the terms in h tend to zero.</p> <p>Therefore $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} = 4x^3$</p> | <p>M1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>E1</p> <p>[5]</p> | <p>1.1</p> <p>1.1</p> <p>1.1</p> <p>2.4</p> <p>2.1</p> | <p>Attempt at expansion with product of powers of x and h summing to 4 and some attempt at coefficients, not necessarily correct</p> <p>Attempt $\frac{f(x+h) - f(x)}{h}$</p> <p>Allow at most two errors</p> <p>All terms correct</p> <p>Accept some indication that as h tends to 0, the terms involving h vanish and leave $4x^3$</p> <p>Award for good use of language, and of limit and function notation</p> <p>Only requires the two M1 marks to be awarded.</p> |

| Question | Answer | Marks | AOs | Guidance |
|----------|--|--|--|---|
| 8 | $2x + 3y = 0$ $\Rightarrow y = -\frac{2}{3}x$ and gradient $-\frac{2}{3}$ Hence, gradient of the tangent is $\frac{3}{2}$ $\frac{dy}{dx} = \frac{3}{2}kx^{\frac{1}{2}}$ At $x = 4$, $\frac{3}{2}k(4)^{\frac{1}{2}} = 3k$ Hence $3k = \frac{3}{2}$, so $k = \frac{1}{2}$ At P , $y = \frac{1}{2}(4)^{\frac{3}{2}} = 4$ so $P = (4, 4)$ so equation of normal through P is $(y - 4) = -\frac{2}{3}(x - 4)$ When $y = 0$, $x = 10$ so $Q = (10, 0)$ Using $P(4, 4)$ and $Q(10, 0)$ $PQ^2 = (10 - 4)^2 + (0 - 4)^2$ Circle equation is $(x - 4)^2 + (y - 4)^2 = 52$ | <p>M1</p> <p>A1FT</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>E1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1FT</p> <p>[10]</p> | <p>3.1a</p> <p>1.1</p> <p>1.1a</p> <p>1.1</p> <p>1.1</p> <p>1.1</p> <p>3.1a</p> <p>1.1</p> <p>1.1</p> <p>1.1</p> | <p>Identify gradient of line $(= -\frac{2}{3})$ anywhere</p> <p>Use $m_1m_2 = -1$ anywhere $(= \frac{3}{2})$ FT their gradient</p> <p>Attempt differentiation</p> <p>Obtain $\frac{3}{2}kx^{\frac{1}{2}}$</p> <p>Substitute $x = 4$ and equate to the normal gradient</p> <p>AG</p> <p>Identify coordinates, gradient of normal and form equation with their coordinates</p> <p>Substitute $y = 0$ and obtain $x = 10$</p> <p>Use Pythagoras to obtain length PQ^2</p> <p>Accept equivalent forms FT their coordinates for P and Q</p> <p>Allow sign slip</p> <p>The power must be seen to decrease</p> <p>Tangent gradients may also be used i.e. $-\frac{1}{3k} = -\frac{2}{3}$</p> <p>Accept $y = 4$</p> |

| Question | | Answer | Marks | AOs | Guidance | |
|----------|-------|---|-------|------|---|---|
| 9 | (i) | $-\left(\frac{4-0}{8-5}\right)$ | M1 | 1.1 | Attempt at acceleration calculation with at most one error | Or use of $v = u + at$ with $v = 0, u = 4$ and $t = 3$ with at least 2 values correct |
| | | Acceleration = $-\frac{4}{3}$ | A1 | 1.1 | Or equivalent | |
| 9 | (ii) | Distance travelled $= \frac{1}{2}(5+8)(4) + \frac{1}{2}(12)(3) = 44$ | M1 | 1.1 | Attempt at both areas; the trapezium and triangle | |
| | | Displacement $= \frac{1}{2}(5+8)(4) - \frac{1}{2}(12)(3) = 8$ | A1 | 1.1 | Either distance travelled or displacement correct | |
| | | 44 m > 40 m so distance travelled is more than five times the displacement | E1 | 2.2a | Must see relevant comparison | |
| | | | [3] | | | |
| 10 | (i) | $s = 9(6)^2 - 1.5(6)^3 = 0$ | M1 | 1.1 | | |
| | | E.g. The boomerang is at O E.g. She catches the boomerang | E1 | 3.4 | | |
| | | | [2] | | | |
| 10 | (ii) | $v = 18t - \frac{9}{2}t^2$ | M1 | 1.1 | | |
| | | When $v = 0$, $t = 0$ or $t = 4$ | M1 | 1.1 | Imply deduction that greatest distance is when velocity = 0 and solve | |
| | | At $t = 0$, $s = 0$, so maximum displacement must be when $t = 4$ giving $s = 48$ m | A1 | 1.1 | | |
| | | | E1 | 3.4 | | |
| | | [4] | | | | |
| 10 | (iii) | $t = 5$ | B1 | 3.1b | | |
| | | $v = -22.5$ | B1 | 3.4 | | |
| | | | [2] | | | |
| 10 | (iv) | $a = 18 - 9t$ | M1 | 1.1 | | |
| | | Acceleration = -27 (ms ⁻²) | A1 | 1.1 | | |
| | | | [2] | | | |

| Question | | Answer | Marks | AOs | Guidance | | | | |
|----------|-------|--|-------|------|--|---|---|--|---|
| 11 | (i) | Resultant force from the tug boats is positive so it is moving east | E1 | 2.2a | (600i) | | | | |
| | | There is zero resultant force in the j direction, so it is not moving north or south | E1 | 2.2a | | | | | |
| | | | [2] | | | | | | |
| 11 | (ii) | $350 + 250 - 200 = 100000a$ | M1 | 3.3 | Use $F = ma$. Allow sign errors and one missing force | | | | |
| | | Obtain 0.004 m s^{-2} | A1 | 1.1 | | | | | |
| | | | [2] | | | | | | |
| 11 | (iii) | $400 = 1.5t + \frac{1}{2}(0.004)t^2$ | M1 | 3.1b | Use $s = ut + \frac{1}{2}at^2$ | | | | |
| | | $0.002t^2 + 1.5t - 400 = 0$ | A1 | 1.1 | | Obtain correct quadratic. Any equivalent form | | | |
| | | Obtain 209 (seconds) | M1 | 3.4 | | | Use any method to solve their quadratic | | |
| | | $v^2 = 1.5^2 + 2(0.004)(400)$ | A1 | 1.1 | | | | If negative root given (-958.63088) this must be clearly discarded | |
| | | Obtain $2.33 \text{ (m s}^{-1}\text{)}$ | M1 | 3.4 | | | | | Use $v^2 = u^2 + 2as$ with their a or $v = u + at$ with their a and t |
| | | | A1 | 1.1 | | | | | |
| | [6] | | | | | | | | |

Assessment Objectives (AO) Grid

| Question | AO1 | AO2 | AO3(PS) | AO3(M) | Total |
|------------------|-----------|-----------|----------|-----------|-----------|
| Pure | | | | | |
| 1(i)(a) | 2 | | | | 2 |
| 1(i)(b) | 1 | | | | 1 |
| 1(ii)(a) | 1 | | | | 1 |
| 1(ii)(b) | 1 | | | | 1 |
| 2 | 4 | | 1 | | 5 |
| 3(i) | 1 | 1 | | | 2 |
| 3(ii) | 1 | | | | 1 |
| 3(iii) | 2 | | | 1 | 3 |
| 3(iv) | | | | 1 | 1 |
| 4(i) | 2 | | 1 | | 3 |
| 4(ii) | 2 | 1 | | | 3 |
| 5(i) | | 2 | | | 2 |
| 5(ii) | 2 | | | 1 | 3 |
| 5(iii) | | | | 2 | 2 |
| 6(i) | | 2 | | | 2 |
| 6(ii) | 1 | 2 | | | 3 |
| 7 | 3 | 2 | | | 5 |
| 8 | 8 | | 2 | | 10 |
| | | | | | |
| Mechanics | | | | | |
| 9(i) | 2 | | | | 2 |
| 9(ii) | 2 | 1 | | | 3 |
| 10(i) | 1 | | | 1 | 2 |
| 10(ii) | 3 | | | 1 | 4 |
| 10(iii) | | | 1 | 1 | 2 |
| 11(i) | | 2 | | | 2 |
| 11(ii) | 1 | | | 1 | 2 |
| 11(iii) | 3 | | 1 | 2 | 6 |
| Totals | 45 | 13 | 6 | 11 | 75 |

PS = Problem Solving

M = Modelling

AS Level Mathematics A H230/02 Pure Mathematics and Mechanics Printed Answer Booklet

Date – Morning/Afternoon

Time allowed: 1 hour 30 minutes

OCR supplied materials:

- Printed Answer Booklet

You must have:

- Printed Answer Booklet
- Scientific or graphical calculator



First name

Last name

Centre number

Candidate number

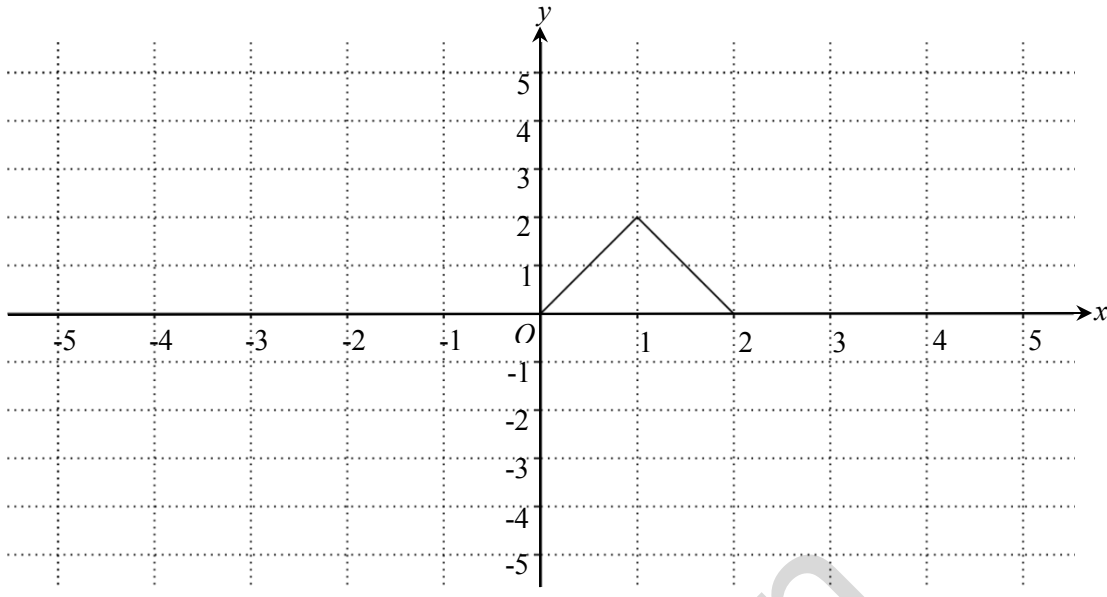
INSTRUCTIONS

- Use black ink. HB pencil may be used for graphs and diagrams only.
- Complete the boxes provided on the Printed Answer Booklet with your name, centre number and candidate number.
- Answer all the questions.
- **Write your answer to each question in the space provided in the Printed Answer Booklet.**
- Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Do **not** write in the bar codes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.
- The acceleration due to gravity is denoted by $g \text{ m s}^{-2}$. Unless otherwise instructed, when a numerical value is needed, use $g = 9.8$.

INFORMATION

- **You are reminded of the need for clear presentation in your answers.**
- The Printed Answer Booklet consists of **12** pages. The Question Paper consists of **8** pages.

Section A: Pure Mathematics

| | |
|------------------------|--|
| <p>1(i)(a)</p> |  |
| <p>1(i)(b)</p> | |
| <p>1(ii)(a)</p> | |
| <p>1(ii)(b)</p> | |

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| 3(i) | |
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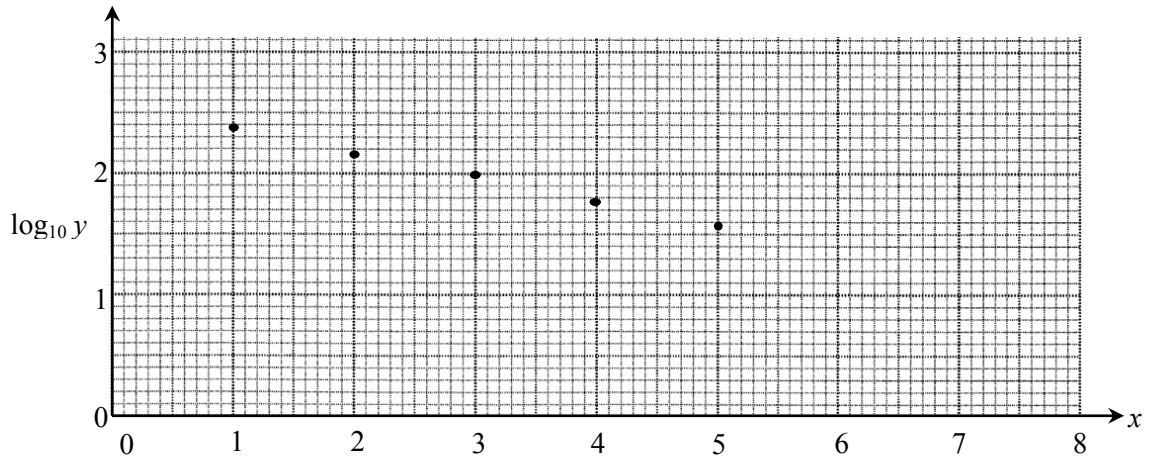
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Section B: Mechanics

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